Exercise 34

Find the critical numbers of the function.

g(t) = |3t - 4|

Solution

A critical number is a value of t for which the derivative is zero or nonexistent. Take the derivative of the function.

$$g'(t) = \frac{d}{dt} |3t - 4|$$

$$= \frac{d}{dt} \sqrt{(3t - 4)^2}$$

$$= \frac{1}{2} [(3t - 4)^2]^{-1/2} \cdot \frac{d}{dt} (3t - 4)^2$$

$$= \frac{1}{2} [(3t - 4)^2]^{-1/2} \cdot 2(3t - 4)^1 \cdot \frac{d}{dt} (3t - 4)$$

$$= \frac{1}{2} [(3t - 4)^2]^{-1/2} \cdot 2(3t - 4) \cdot (3)$$

$$= \frac{6(3t - 4)}{2\sqrt{(3t - 4)^2}}$$

$$= \frac{3(3t - 4)}{|3t - 4|}$$

$$= 3 \operatorname{sgn}(3t - 4)$$

Set what's in the denominator equal to zero and solve for t.

$$|3t - 4| = 0$$
$$3t - 4 = 0$$
$$t = \frac{4}{3}$$